



UNIVERSITY OF WARSAW
Faculty of Economic Sciences

Exchange Rates I: The Monetary Approach in the Long Run Part 1

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Introduction

The goal of this lecture is to set out the long-run relationships between money, prices, and exchange rates.

The theory we will develop has two parts:

- The first involves the theory of purchasing power, linking the exchange rate to price levels in each country in the long run.
- The second involves how price levels are related to monetary conditions in each country.
- Combining the monetary and purchasing power theories we will develop a long-run theory known as the **monetary approach to exchange rates**.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Arbitrage can occur in international goods markets just as in international financial markets. Therefore, the prices of goods in different countries expressed in a common currency may have a tendency to be equalized.

- Applied to a single good, this type of equalization is referred to as the **law of one price**.
- Applied to an entire basket of goods, it is called the theory of **purchasing power parity**.
- We will develop a simple theory based on an idealized world of *frictionless trade* where transaction costs can be neglected.
- We start with single goods and the law of one price then move baskets of goods and purchasing power parity.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

The Law of One Price

The law of one price (**LOOP**) states that in the absence of trade frictions and under free competition and price flexibility, identical goods sold in different locations must sell for the same price when expressed in a common currency.

We can state the law of one price as follows, for the case of any good g sold in two locations:

$$\underbrace{q_{US/EUR}^g}_{\text{Relative price of goods } g \text{ in Europe versus U.S.}} = \underbrace{\left(E_{\$/\epsilon} P_{EUR}^g \right)}_{\text{European price of goods } g \text{ in \$}} / \underbrace{P_{US}^g}_{\text{U.S. price of good } g \text{ in \$}}$$

where $E_{\$/\epsilon}$ is the exchange rate, and LOOP holds if and only if this expression is equal to 1.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

The Law of One Price

We can rearrange the equation for price equality

$$E_{\$/\epsilon} P_{EUR}^g = P_{US}^g$$

to show that the exchange rate must equal the ratio of the goods' prices expressed in the two currencies:

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange rate}} = \underbrace{P_{US}^g / P_{EUR}^g}_{\text{Ratio of goods' prices}}$$

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Purchasing Power Parity

The principle of purchasing power parity (**PPP**) is the macroeconomic counterpart to the microeconomic law of one price (LOOP). To express PPP algebraically, we can compute the relative price of the two baskets of goods in each location:

$$\underbrace{q_{US/EUR}}_{\substack{\text{Relative price} \\ \text{of basket} \\ \text{in Europe} \\ \text{versus U.S.}}} = \underbrace{(E_{\$/\epsilon} P_{EUR})}_{\substack{\text{European price} \\ \text{of basket} \\ \text{expressed} \\ \text{in \$}}} / \underbrace{P_{US}}_{\substack{\text{U.S. price} \\ \text{of basket} \\ \text{expressed} \\ \text{in \$}}}$$

- There is no arbitrage when the basket is the same price in both locations, that is, when $q_{US/EUR} = 1$.
- PPP then holds: price levels in two countries are equal when expressed in a common currency. This is called **absolute PPP**.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

The Real Exchange Rate

The **real exchange rate** is the relative price of the baskets.

- The U.S. real exchange rate $q_{US/EUR} = E_{\$/\epsilon} P_{EUR} / P_{US}$ tells us how many U.S. baskets are needed to purchase one European basket.
- The exchange rate for currencies is a *nominal* concept. The real exchange rate is a *real* concept.

The real exchange rate has terminology similar to the nominal exchange rate:

- If the real exchange rate rises (more Home goods are needed in exchange for Foreign goods), Home has experienced a **real depreciation**.
- If the real exchange rate falls, Home has experienced a **real appreciation**.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Absolute PPP and the Real Exchange Rate

Purchasing power parity (Absolute PPP) requires that the real exchange rate $q_{US/EUR}$ is equal to 1.

- If the real exchange rate $q_{US/EUR}$ is below 1, then Foreign (European) goods are cheap relative to Home (U.S.) goods.
 - In this case, the U.S. dollar is said to be *strong*, the euro is *weak*, and we say the euro is **undervalued**.
- If the real exchange rate $q_{US/EUR}$ is above 1, then Foreign goods are relatively expensive.
 - In this case, the U.S. dollar is said to be *weak*, the euro is *strong*, and we say the euro is **overvalued**.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Absolute PPP, Prices, and the Nominal Exchange Rate

We can rearrange the no-arbitrage equation for the equality of price levels, $E_{\$/\epsilon} P_{EUR} = P_{US}$ to allow us to solve for the exchange rate that would be implied by absolute PPP:

Absolute PPP:

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange rate}} = \underbrace{P_{US} / P_{EUR}}_{\text{Ratio of price levels}} \quad (3-1)$$

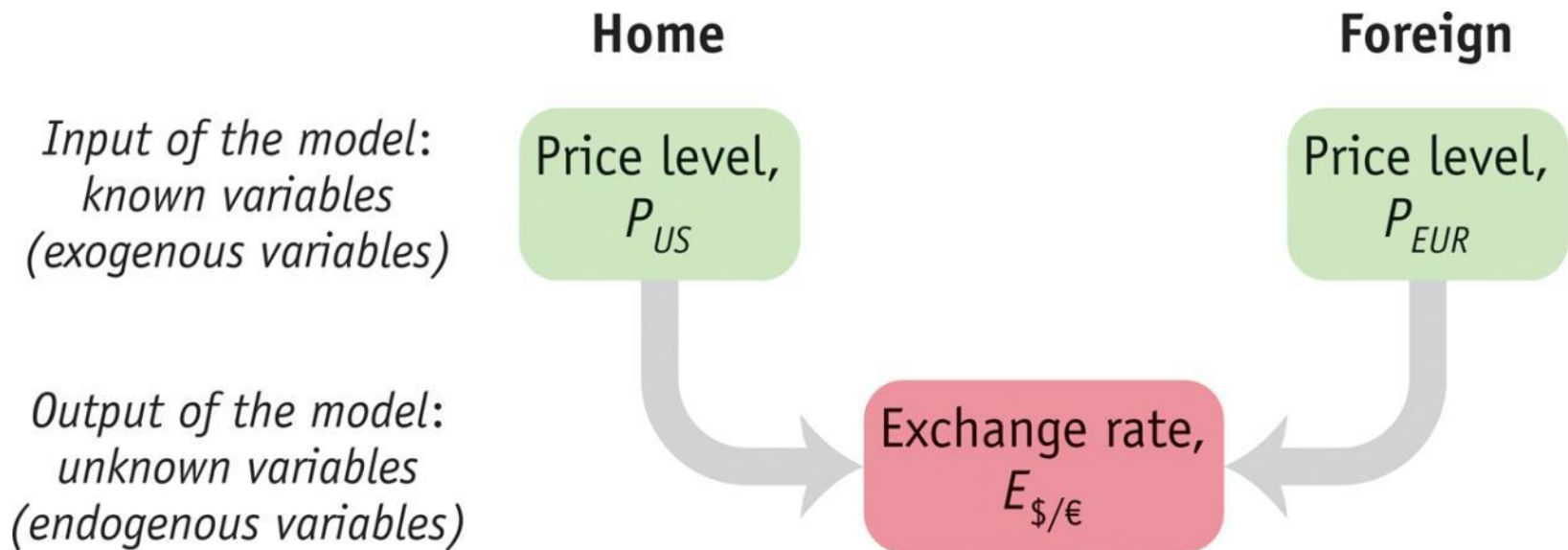
Exchange rate Ratio of price levels

Purchasing power parity implies that the exchange rate at which two currencies trade equals the relative price levels of the two countries.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Absolute PPP, Prices, and the Nominal Exchange Rate

FIGURE 3-1



Building Block: Price Levels and Exchange Rates in the Long Run According to the PPP Theory In this model, the price levels are treated as known exogenous variables (in the green boxes). The model uses these variables to predict the unknown endogenous variable (in the red box), which is the exchange rate.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Relative PPP, Inflation, and Exchange Rate Depreciation

We now examine the implications of PPP for the study of **inflation** (the rate of change of the price level) using 3-1.

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange rate}} = \underbrace{P_{US} / P_{EUR}}_{\text{Ratio of price levels}} \quad (3-1)$$

Exchange rate Ratio of price levels

On the left-hand side, the rate of change of the exchange rate in Home is the rate of exchange rate depreciation in Home given by

$$\frac{\Delta E_{\$/\epsilon,t}}{E_{\$/\epsilon,t}} = \underbrace{\frac{E_{\$/\epsilon,t+1} - E_{\$/\epsilon,t}}{E_{\$/\epsilon,t}}}_{\text{Rate of depreciation of the nominal exchange rate}}$$

Rate of depreciation
of the nominal exchange rate

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Relative PPP, Inflation, and Exchange Rate Depreciation

We now examine the implications of PPP for the study of **inflation** (the rate of change of the price level) using 3-1.

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange rate}} = \underbrace{P_{US} / P_{EUR}}_{\text{Ratio of price levels}} \quad (3-1)$$

Exchange rate Ratio of price levels

On the right, the rate of change of the ratio of price levels equals the rate of change of the numerator minus that of the denominator:

$$\begin{aligned} \frac{\Delta(P_{US}/P_{EUR})}{(P_{US}/P_{EUR})} &= \frac{\Delta P_{US,t}}{P_{US,t}} - \frac{\Delta P_{EUR,t}}{P_{EUR,t}} = \\ &= \underbrace{\left(\frac{P_{US,t+1} - P_{US,t}}{P_{US,t}} \right)}_{\text{Ratio of inflation U.S.}} - \underbrace{\left(\frac{P_{EUR,t+1} - P_{EUR,t}}{P_{EUR,t}} \right)}_{\text{Ratio of inflation Europe}} = \pi_{US,t} - \pi_{EUR,t} \end{aligned}$$

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

Relative PPP, Inflation, and Exchange Rate Depreciation

If Equation (3-1) holds for *levels* of exchange rates and prices, then it must also hold for *rates of change* in these variables. By combining the last two expressions, we obtain:

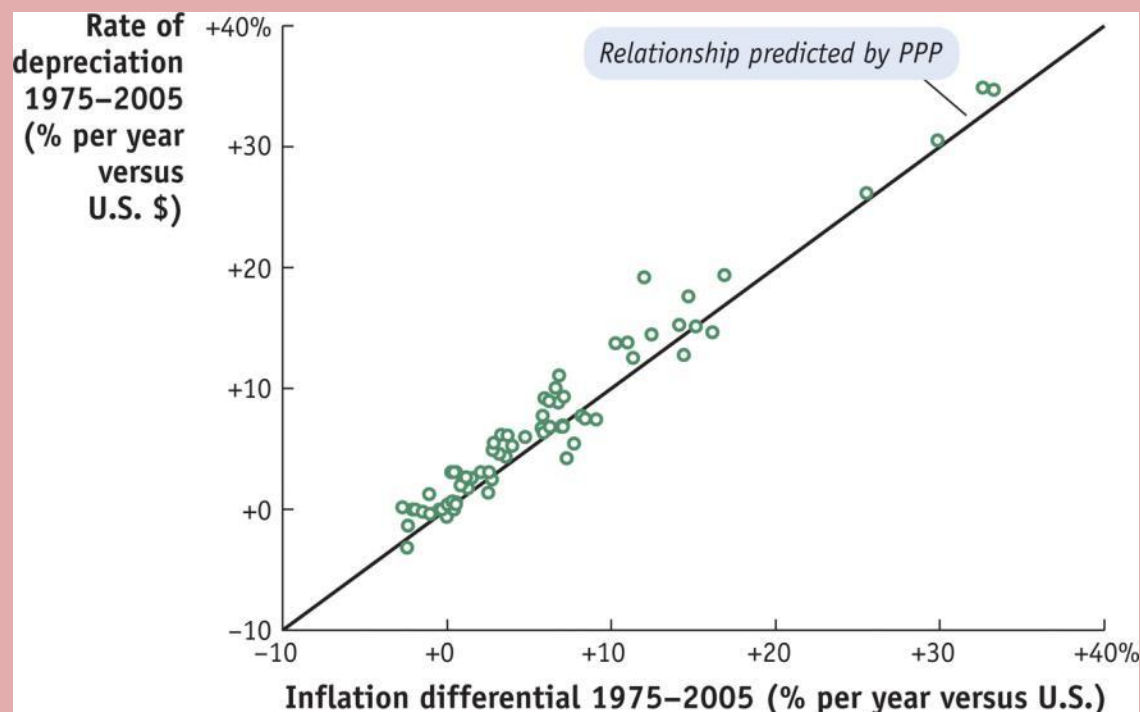
$$\underbrace{\frac{\Delta E_{\$/\epsilon,t}}{E_{\$/\epsilon,t}}}_{\text{Rate of depreciation of the nominal exchange rate}} = \underbrace{\pi_{US,t} - \pi_{EUR,t}}_{\text{Inflation differential}} \quad (3-2)$$

This way of expressing PPP is called **relative PPP**, and it implies that the rate of depreciation of the nominal exchange rate equals the difference between the inflation rates of two countries.

APPLICATION

Evidence for PPP in the Long Run and Short Run

FIGURE 3-2

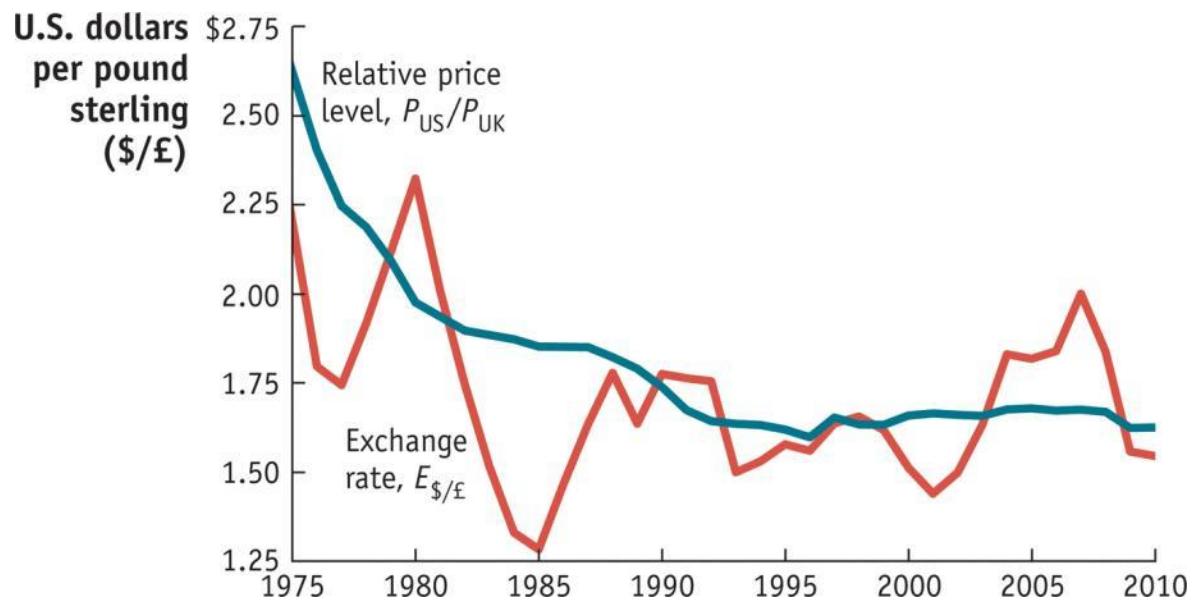


Inflation Differentials and the Exchange Rate, 1975–2005 This scatterplot shows the relationship between the rate of exchange rate depreciation against the U.S. dollar and the inflation differential against the United States over the long run, for a sample of 82 countries. The correlation between the two variables is strong and bears a close resemblance to the prediction of PPP that all data points would appear on the 45-degree line.

APPLICATION

Evidence for PPP in the Long Run and Short Run

FIGURE 3-3



Exchange Rates and Relative Price Levels Data for the United States and the UK from 1975 to 2010 show that the exchange rate and relative price levels do not always move together in the short run. Relative price levels tend to change slowly and have a small range of movement; exchange rates move quickly and experience large fluctuations. Therefore, relative PPP does *not* hold in the short run. It is a better guide to the long run, and we can see that the two series do tend to drift together over the decades.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

How Slow Is Convergence to PPP?

- Research shows that price differences—the deviations from PPP—can be quite persistent.
- Estimates suggest that these deviations may die out at a rate of about 15% per year. This kind of measure is often called a *speed of convergence*.
- Approximately half of any PPP deviation still remains after four years: Economists refer to this as a four-year *half-life*.
- Such estimates provide a rule of thumb that is useful as a guide to forecasting real exchange rates.

Forecasting when the Real Exchange Rate Is Undervalued or Overvalued

- When relative PPP holds, forecasting exchange rate changes is simple: Just compute the inflation differential.
- But how do we forecast when PPP doesn't hold, as is often the case? Knowing the real exchange rate and the convergence speed may still allow us to construct a forecast of real and nominal exchange rates.
- The rate of change of the nominal exchange rate equals the rate of change of the real exchange rate plus home inflation minus foreign inflation:

$$\underbrace{\frac{\Delta E_{\$/\epsilon,t}}{E_{\$/\epsilon,t}}}_{\text{Rate of depreciation on of the nominal exchange rate}} = \underbrace{\frac{\Delta q_{US/EUR,t}}{q_{US/EUR,t}}}_{\text{Rate of depreciation of the real exchange rate}} + \underbrace{\pi_{US,t} - \pi_{EUR,t}}_{\text{Inflation differential}}$$

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

What Explains Deviations from PPP?

There could be a variety of reasons PPP fails in the short run:

- *Transaction costs.* These include costs of transportation, tariffs, duties, and other costs due to shipping and delays associated with developing distribution networks and satisfying legal and regulatory requirements in foreign markets. On average, they are more than 20% of the price of goods traded internationally.
- *Nontraded goods.* Some goods are inherently nontradable; they have infinitely high transaction costs. Most goods and services fall somewhere between tradable and nontradable.

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

What Explains Deviations from PPP?

- *Imperfect competition and legal obstacles.* Many goods are not simple undifferentiated commodities, as LOOP and PPP assume. Differentiated goods create conditions of *imperfect competition* because firms have some power to set the price of their good, allowing firms to charge different prices not just across brands but also across countries.
- *Price stickiness.* Prices do not or cannot adjust quickly and flexibly to changes in market conditions.

HEADLINES

The Big Mac Index

For more than 25 years, *The Economist* newspaper has engaged in a whimsical attempt to judge PPP theory based on a well-known, globally uniform consumer good: the McDonald's Big Mac. The over- or undervaluation of a currency against the U.S. dollar is gauged by comparing the relative prices of a burger in a common currency, and expressing the difference as a percentage deviation from one:

$$\text{Big Mac Index} = q^{\text{Big Mac}} - 1 = \left(\frac{E_{\$/\text{local currency}} P_{\text{local}}^{\text{Big Mac}}}{P_{\text{US}}^{\text{Big Mac}}} \right) - 1$$



Home of the undervalued burger?

AP Photo/Greg Baker

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

TABLE 3-1 (1 of 3)

The Big Mac Index

The table shows the price of a Big Mac in January 2016 in local currency (column 1) and converted to U.S. dollars (column 2) using the actual exchange rate (column 4). The dollar price can then be compared with the average price of a Big Mac in the United States (\$4.93 in column 1, row 1). The difference (column 5) is a measure of the overvaluation (+) or undervaluation (–) of the local currency against the U.S. dollar. The exchange rate against the dollar implied by PPP (column 3) is the hypothetical price of dollars in local currency that would have equalized burger prices, which may be compared with the actual observed exchange rate (column 4).

	BIG MAC PRICES		EXCHANGE RATE (LOCAL CURRENCY PER U.S. DOLLAR)		Overvaluation (+) / Undervaluation (–) Against U.S. Dollar, % (5)
	In Local Currency (1)	In U.S. Dollars (2)	Implied by PPP (3)	Actual, July 25th (4)	
United States	\$ 4.93	4.93	—	—	—
Argentina	Peso 33	2.39	6.69	13.81	–52
Australia	A\$ 5.3	3.74	1.08	1.42	–24
Brazil	Real 13.5	3.35	2.74	4.02	–32
Britain	£ 2.89	4.22	0.59	0.68	–14
Canada	C\$ 5.84	4.14	1.18	1.41	–15
Chile	Peso 2100	2.94	425.96	715.05	–40
China	Yuan 17.6	2.68	3.57	6.56	–46
Colombia	Peso 7900	2.43	1602.43	3253.9	–51
Costa Rica	Colones 2150	4.02	436.11	535.25	–19
Czech Republic	Koruna 75	2.98	15.21	25.14	–39

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

TABLE 3-1 (2 of 3)

The Big Mac Index (continued)

	Big Mac Prices		Exchange rate (local currency per U.S. dollar)		Over (+)/ under (-) valuation against dollar, %
	In local currency (1)	In U.S. dollars (2)	Implied by PPP (3)	Actual, July 25th (4)	
Denmark	DK 30	4.32	6.09	6.94	-12
Egypt	Pound 16.93	2.16	3.42	7.83	-56
Euro area	€ 3.72	4.99	0.75	0.93	-19
Hong Kong	HK\$ 19.2	2.48	3.89	7.75	-50
Hungary	Forint 900	3.08	182.56	292.68	-38
India	Rupee 127	1.90	25.76	66.80	-61
Indonesia	Rupiah 30500	2.19	6186.6	13947.5	-55
Israel	Shekel 16.9	4.29	3.43	3.94	-13
Japan	Yen 370	3.12	75.05	118.65	-37
Malaysia	Ringgit 8	1.82	1.62	4.39	-63
Mexico	Peso 49	2.81	9.94	17.44	-43
New Zealand	NZ\$ 5.9	3.91	1.20	1.51	-21
Norway	Kroner 46.8	5.21	9.49	8.97	6
Pakistan	Rupee 300	2.86	60.85	104.89	-42

1 Exchange Rates and Prices in the Long Run: Purchasing Power Parity and Goods Market Equilibrium

TABLE 3-1 (3 of 3)

The Big Mac Index (continued)

	Big Mac Prices		Exchange rate (local currency per U.S. dollar)		Over (+)/ under (-) valuation against dollar, %
	In local currency (1)	In U.S. dollars (2)	Implied by PPP (3)	Actual, July 25th (4)	
Philippines	Peso 131	2.79	26.57	47.02	-43
Poland	Zloty 9.6	2.37	1.95	4.05	-52
Russia	Rouble 114	1.53	23.12	74.66	-69
Saudi Arabia	riyal 12	3.20	2.43	3.75	-35
Singapore	S\$ 4.7	3.27	0.95	1.44	-34
South Africa	Rand 28	1.77	5.68	15.81	-64
South Korea	Won 4300	3.59	872.21	1197.75	-27
Sri Lanka	Rupee 350	2.43	70.99	144.05	-50
Sweden	SKr 45	5.23	9.13	8.6	6
Switzerland	SFr 6.5	6.44	1.32	1.01	31
Taiwan	NT\$ 112	3.08	14.00	33.23	-57
Thailand	Baht 112	3.09	22.72	36.22	-37
Turkey	Lira 10.25	3.41	2.08	3.01	-30
UAE	Dirhams 13	3.54	2.64	3.67	-28
Ukraine	Hryvnia 36	1.54	7.30	23.35	-69
Uruguay	Peso 113	3.74	22.92	30.19	-24
Venezuela	Bolivar 132	0.66	26.77	198.7	-87

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

- In the long run the exchange rate is determined by the ratio of the price levels in two countries. But this prompts a question: *What determines those price levels?*
- Monetary theory supplies an answer: In the long run, price levels are determined in each country by the relative demand and supply of money.
- This section recaps the essential elements of monetary theory and shows how they fit into our theory of exchange rates in the long run.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

What Is Money?

Economists think of **money** as performing three key functions in an economy:

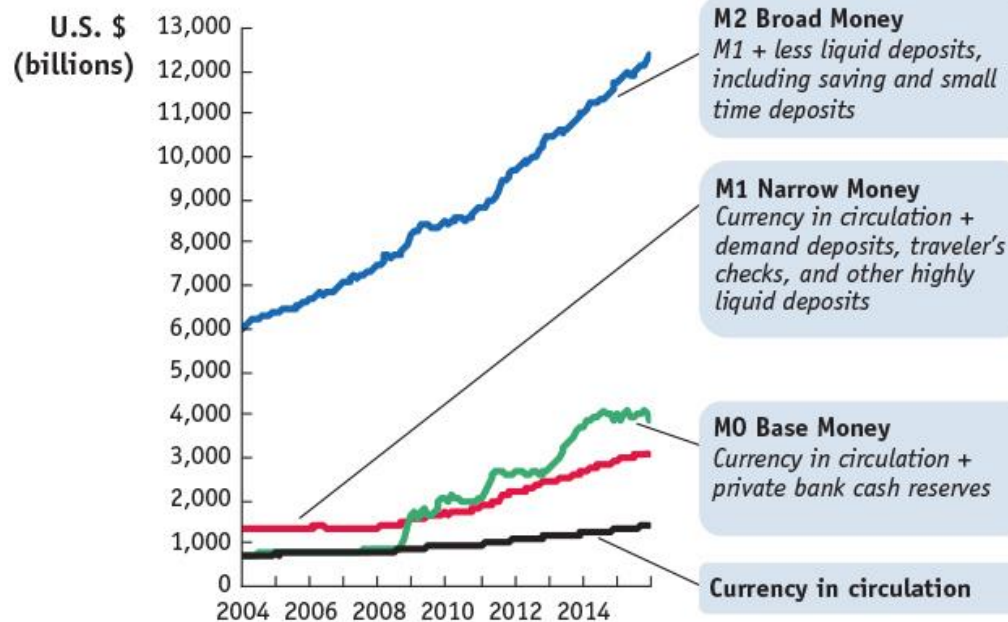
1. Money is a *store of value* because it can be used to buy goods and services in the future. If the opportunity cost of holding money is low, we will hold money more willingly than we hold other assets.
2. Money also gives us a *unit of account* in which all prices in the economy are quoted.
3. Money is a *medium of exchange* that allows us to buy and sell goods and services without the need to engage in inefficient barter.

2 Money, Prices, and Exchange Rates in the Long Run: Money

Market Equilibrium in a Simple Model

The Measurement of Money

FIGURE 3-4



The Measurement of Money This figure shows the major kinds of monetary aggregates (currency, M0, M1, and M2) for the United States from 2004 to 2015. Normally, bank reserves are very close to zero, so M0 and currency are virtually identical, but reserves spiked up during the financial crisis in 2008, as private banks sold securities to the Fed and stored up the cash proceeds in their Fed reserve accounts.

The Supply of Money: In practice, a country's **central bank** controls the **money supply**. We make the simplifying assumption that the central bank's indirectly, but accurately, control the level of M1.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

The Demand for Money: A Simple Model

- We assume **money demand** is motivated by the need to conduct transactions in proportion to an individual's income and we infer that the aggregate money demand will behave similarly (known as the **quantity theory of money**).

$$\underbrace{M^d}_{\text{Demand for money (\$)}} = \underbrace{\bar{L}}_{\text{A constant}} \times \underbrace{P Y}_{\text{Nominal income (\$)}}$$

- All else equal, a rise in national dollar income (nominal income) will cause a proportional increase in transactions and in aggregate money demand.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

The Demand for Money: A Simple Model

- Dividing the previous equation by P , the price level, we can derive the *demand for real money balances*:

$$\underbrace{\frac{M^d}{P}}_{\text{Demand for real money}} = \underbrace{\bar{L}}_{\text{A constant}} \times \underbrace{Y}_{\text{Real income}}$$

- Real money balances are simply a measure of the purchasing power of the stock of money in terms of goods and services. The demand for real money balances is strictly proportional to real income.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Equilibrium in the Money Market

- The condition for equilibrium in the money market is simple to state: The demand for money M^d must equal the supply of money M , which we assume to be under the control of the central bank.
- Imposing this condition on the last two equations, we find that nominal money supply equals nominal money demand:

$$M = \bar{L} P Y$$

and, equivalently, that real money supply equals real money demand:

$$\frac{M}{P} = \bar{L} Y$$

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

A Simple Monetary Model of Prices

- Expressions for the price levels in the United States and Europe are:

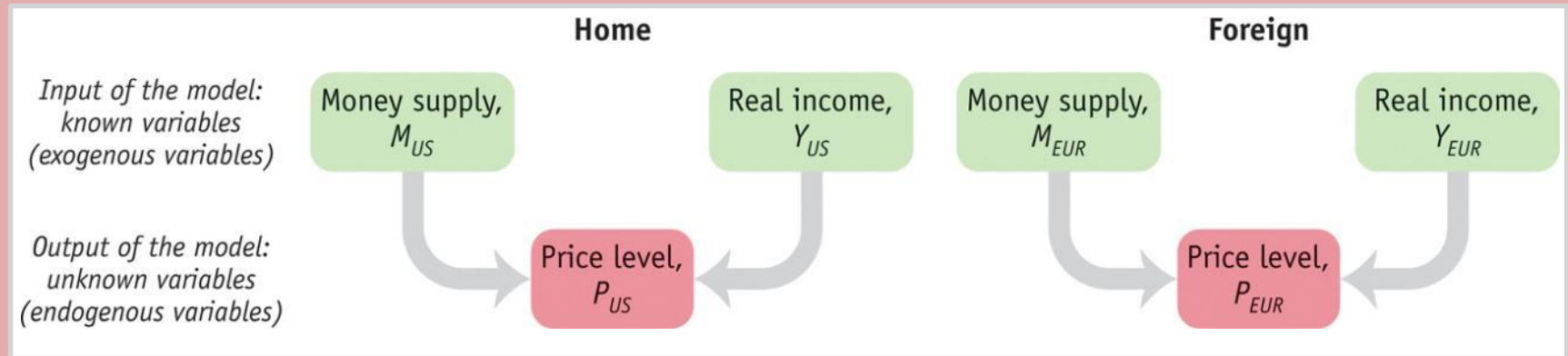
$$P_{US} = \frac{M_{US}}{\bar{L}_{US} Y_{US}} \qquad P_{EUR} = \frac{M_{EUR}}{\bar{L}_{EUR} Y_{EUR}}$$

- These two equations are examples of the **fundamental equation of the monetary model of the price level**.
- In the long run, we assume prices are flexible and will adjust to put the money market in equilibrium.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

A Simple Monetary Model of Prices

FIGURE 3-5



Building Block: The Monetary Theory of the Price Level According to the Long-Run Monetary Model In these models, the money supply and real income are treated as known exogenous variables (in the green boxes). The models use these variables to predict the unknown endogenous variables (in the red boxes), which are the price levels in each country.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

A Simple Monetary Model of the Exchange Rate

Plugging the expression for the price level in the monetary model to Equation (3-1), we can use absolute PPP to solve for the exchange rate:

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange Rate}} = \underbrace{\frac{P_{US}}{P_{EUR}}}_{\text{Ratio of price levels}} = \frac{\left(\frac{M_{US}}{\bar{L}_{US}Y_{US}}\right)}{\left(\frac{M_{EUR}}{\bar{L}_{EUR}Y_{EUR}}\right)} = \frac{(M_{US}/M_{EUR})}{\underbrace{(\bar{L}_{US}Y_{US}/\bar{L}_{EUR}Y_{EUR})}_{\text{Relative nominal money supplies divided by relative real money demands}}} \quad (3-3)$$

This is the fundamental equation of the monetary approach to exchange rates.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

The implications of the fundamental equation of the monetary approach to exchange rates are intuitive.

- Suppose the U.S. money supply increases, all else equal. The right-hand side increases (the U.S. nominal money supply increases relative to Europe), causing the exchange rate to increase (the U.S. dollar depreciates against the euro).

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange Rate}} = \underbrace{\frac{P_{US}}{P_{EUR}}}_{\text{Ratio of price levels}} = \frac{\left(\frac{M_{US}}{\bar{L}_{US}Y_{US}}\right)}{\left(\frac{M_{EUR}}{\bar{L}_{EUR}Y_{EUR}}\right)} = \underbrace{\frac{(M_{US}/M_{EUR})}{(\bar{L}_{US}Y_{US}/\bar{L}_{EUR}Y_{EUR})}}_{\text{Relative nominal money supplies divided by relative real money demands}}$$

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

The implications of the fundamental equation of the monetary approach to exchange rates are intuitive.

- Now suppose the U.S. real income level increases, all else equal. Then the right-hand side decreases (the U.S. real money demand increases relative to Europe), causing the exchange rate to decrease (the U.S. dollar appreciates against the euro).

$$\underbrace{E_{\$/\epsilon}}_{\text{Exchange Rate}} = \underbrace{\frac{P_{US}}{P_{EUR}}}_{\text{Ratio of price levels}} = \frac{\left(\frac{M_{US}}{\bar{L}_{US}Y_{US}}\right)}{\left(\frac{M_{EUR}}{\bar{L}_{EUR}Y_{EUR}}\right)} = \frac{(M_{US}/M_{EUR})}{\underbrace{(\bar{L}_{US}Y_{US}/\bar{L}_{EUR}Y_{EUR})}_{\text{Relative nominal money supplies divided by relative real money demands}}}$$

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

The U.S. money supply is M_{US} , and its growth rate is μ_{US} :

$$\mu_{US,t} = \underbrace{\frac{M_{US,t+1} - M_{US,t}}{M_{US,t}}}$$

Rate of money supply growth in U.S.

The growth rate of real income in the U.S. is g_{US} :

$$g_{US,t} = \underbrace{\frac{Y_{US,t+1} - Y_{US,t}}{Y_{US,t}}}$$

Rate of real income growth in U.S.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

Therefore, the growth rate of $P_{US} = M_{US} / \bar{L}_{US} Y_{US}$ equals the money supply growth rate μ_{US} minus the real income growth rate g_{US} . The growth rate of P_{US} is the inflation rate π_{US} . Thus, we know that:

$$\pi_{US,t} = \mu_{US,t} - g_{US,t} \quad (3-4)$$

The rate of change of the European price level is the inflation rate π_{EUR} , and is calculated similarly:

$$\pi_{EUR,t} = \mu_{EUR,t} - g_{EUR,t} \quad (3-5)$$

When money growth is higher than income growth, we have “more money chasing fewer goods” and this leads to inflation.

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

Combining (3-4) and (3-5), we can now solve for the inflation differential in terms of monetary fundamentals and compute the rate of depreciation of the exchange rate:

$$\underbrace{\frac{\Delta E_{\$/\epsilon,t}}{E_{\$/\epsilon,t}}}_{\substack{\text{Rate of depreciation} \\ \text{of the} \\ \text{nominal exchange rate}}} = \underbrace{\pi_{US,t} - \pi_{EUR,t}}_{\text{Inflation differential}} = (\mu_{US,t} - g_{US,t}) - (\mu_{EUR,t} - g_{EUR,t}) \quad (3-6)$$
$$= \underbrace{(\mu_{US,t} - \mu_{EUR,t})}_{\substack{\text{Differential in} \\ \text{nominal money supply} \\ \text{growth rates}}} - \underbrace{(g_{US,t} - g_{EUR,t})}_{\substack{\text{Differential in} \\ \text{real output} \\ \text{growth rates}}}$$

2 Money, Prices, and Exchange Rates in the Long Run: Money Market Equilibrium in a Simple Model

Money Growth, Inflation, and Depreciation

The intuition behind Equation (3-6) is as follows:

- If the United States runs a looser monetary policy in the long run, measured by a faster money growth rate, the dollar will depreciate more rapidly, all else equal.
- If the U.S. economy grows faster in the long run, the dollar will appreciate more rapidly, all else equal.

KEY POINTS

1. Purchasing power parity (PPP) implies that the exchange rate should equal the relative price level in the two countries, and the real exchange rate should equal 1.

KEY POINTS

2. Evidence for PPP is weak in the short run but more favorable in the long run. In the short run, deviations are common and changes in the real exchange rate do occur. The failure of PPP in the short run is primarily the result of market frictions, imperfections that limit arbitrage, and price stickiness.

KEY POINTS

3. A simple monetary model (the quantity theory) explains price levels in terms of money supply levels and real income levels. Because PPP can explain exchange rates in terms of price levels, the two together can be used to develop a monetary approach to the exchange rate.

KEY TERMS

monetary approach to
exchange rates
law of one price (LOOP)
purchasing power parity
(PPP)
absolute PPP
real exchange rate
real depreciation
real appreciation
overvalued
undervalued
inflation
relative PPP

money
central bank
money supply
money demand
quantity theory of money
fundamental equation of
the monetary model of
the price level
fundamental equation of
the monetary approach
to exchange rates
hyperinflation
real money demand
function

Fisher effect
real interest rate
real interest parity
world real interest rate
nominal anchors
monetary regime
exchange rate target
money supply target
inflation target plus
interest rate policy
central-bank
independence

Thank You for your
attention!