# Dynamic Panel Data Part One

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- Penn World Table
- PWT 6.3
- Alan Heston, Robert Summers and Bettina Aten, Penn World Table Version 6.3, Center for International Comparisons of Production, Income and Prices at the University of Pennsylvania, August 2009.
- http://pwt.econ.upenn.edu/php\_site/pwt\_index.php

#### pwt63.dta na stronie.

use "pwt63.dta", clear Countries as a string converted into double: encode country, generate(cty) Panel dimension: xtset cty year

#### Population growth rate:

g popg=(pop-l.pop)/l.pop
Jump variable for every 5 years:
gen num5=int((year-1950)/5+1)

### Mean averaging for every 5 years and collapsing:

collapse (mean) rgdpch ki grgdpch popg, by(cty num5) New panel:

xtset cty num5

#### Decode:

decode cty, generate(Country)

#### Logarithm of GDP:

g lpkb= log(rgdpch)

Growth rate:

g dpkb= log(rgdpch)-log(l.rgdpch)

Technological progress rate plus population growth rate plus depreciation rate:

g pop=popg+0.07

#### describe

	Contains dat	a			
	obs:	2,280			
	vars:	15			
	size:	223,440 (	99.9% of m	emory free)	(_dta has notes)
		storado	display		
	wariahlo nam	—			variable label
	cty	long	%24.0g	Kraj	Country
	num5	float	%9.0g		
	rgdpch	double	%10.0g		(mean) rgdpch
	ki	double	%10.0g		(mean) ki
	grgdpch		%10.0g		(mean) grgdpch
	popg	float	%9.0g		(mean) popg
	Country	str24	%24s		Country
•	lpkb	float	89.0g		
	dpkb	float	89.0g		
	рор	float	%9.0g		
	lagpkp	float	%9.0g		
	lpop	double	%10.0g		
	lki	double	%10.0g		
•	_est_rDFE	byte	88.0g		esample() from estimates store
	_est_DFE	byte	%8.0g		esample() from estimates store
	Sorted by.	ctv num5			
			s changed	since last sav	ved

#### summarize

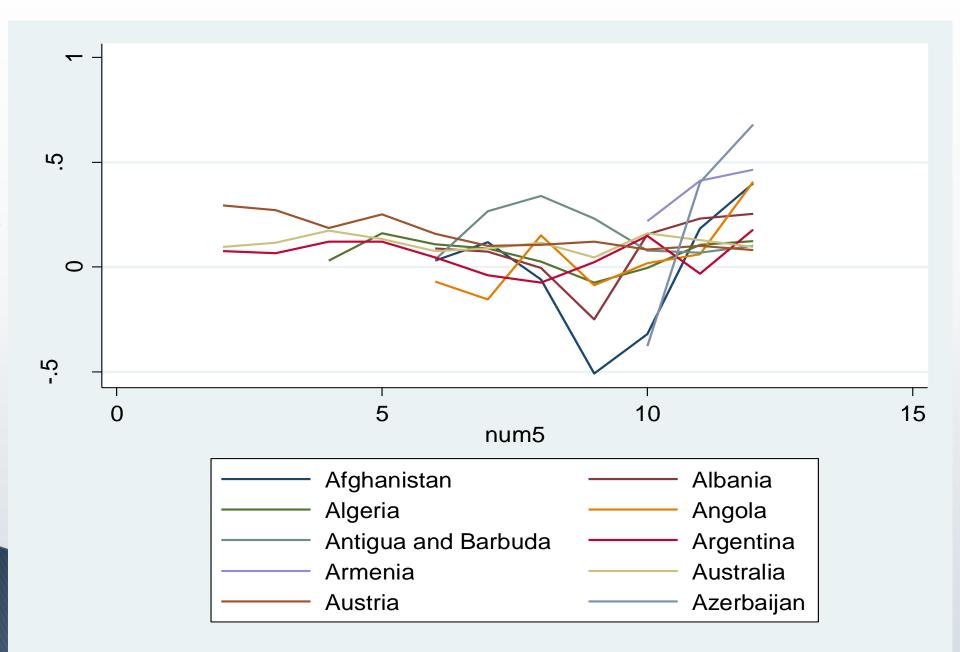
	Variable	Obs	Mean	Std. Dev.	Min	Max
•	+	+				
	cty	2280	95.5	54.85955	1	190
•	num5	2280	6.5	3.45281	1	12
•	rgdpch	1780	8804.549	10935.33	279.9274	90095.22
•	ki	1780	21.46645	12.74437	7724877	91.59714
•	grgdpch	1769	2.267196	4.504332	-31.73853	49.83998
•		+				
•	popg	2280	.0191774	.0142226	0358202	.1578099
•	Country	0				
•	lpkb	1780	8.465461	1.136879	5.634531	11.40862
•	dpkb	1590	.0916539	.1695351	-1.380931	1.258495
•	pop	2280	.0891774	.0142226	.0341798	.2278099

(już z wygenerowanymi, przekształconymi zmiennymi)

#### xtdescribe

•	cty:	1, 2,	., 190			n	=	190
•	num5:	1, 2,	., 12			Т	=	12
•		Delta(nu	um5) = 1 un	it				
•		Span(num	15) = 12 p	eriods				
•		(cty*num	15 uniquely	identifies	each obser	vation)		
•	Distributi	.on of T_i	: min	5% 2	.5% 50	8 758	95%	max
•			12	12	12 1	2 12	12	12
•	Freq.	Percent	Cum.	Pattern				
•			+					
•	190	100.00	100.00	111111111	111			
•			+					
•	190	100.00		XXXXXXXXX	XXXX			
•	Variable	I	Mean	Std. Dev.	Min	Max	Obse	rvations
•		+-				+	+	
•	cty c	overall	95.5	54.85955	1	190	N =	2280
•	b	etween		54.99242	1	190	n =	190
•	W	ithin		0	95.5	95.5	т =	12
•								
•	num5 c	overall	6.5	3.45281	1	12	N =	2280
•	b	etween		0	6.5	6.5	n =	190
•	W	ithin		3.45281	1	12	T =	12
•								
•	rgdpch c	overall	8804.549	10935.33	279.9274	90095.22	N =	1780
×	b	etween		9964.516	567.377	63057.99	n =	190
		ithin		4945.412	-12101.97	52381.56	T-bar =	9.36842
	ki c	overall	21.4	12.74437	7724877	91.59714	N =	1780
	b	etween			3.595346	62.61802	n =	190

#### > xtline dpkb if cty<=10, overlay</pre>





#### xtdescribe

•	cty:	1, 2,	., 190			n	=	190
•	num5:	1, 2,	., 12			Т	=	12
•		Delta(nu	um5) = 1 un	it				
•		Span(num	15) = 12 p	eriods				
•		(cty*num	15 uniquely	identifies	each obser	vation)		
•	Distributi	.on of T_i	: min	5% 2	.5% 50	8 758	95%	max
•			12	12	12 1	2 12	12	12
•	Freq.	Percent	Cum.	Pattern				
•			+					
•	190	100.00	100.00	111111111	111			
•			+					
•	190	100.00		XXXXXXXXX	XXXX			
•	Variable	I	Mean	Std. Dev.	Min	Max	Obse	rvations
•		+-				+	+	
•	cty c	overall	95.5	54.85955	1	190	N =	2280
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	ki c	overall	21.4	12.74437	7724877	91.59714	N =	1780
	b	etween			3.595346	62.61802	n =	190

Cross section 1955-1960

>. reg dpkb l.lpkb pop ki if num5==2

	Source	SS	df	MS		Number of obs	= 67
	+-					F(3, 63)	= 7.31
	Model	.175220322	3.05	8406774		Prob > F	= 0.0003
	Residual	.503661818	63 .00	7994632		R-squared	= 0.2581
	+-					Adj R-squared	= 0.2228
	Total	.67888214	66 .01	0286093		Root MSE	08941
	dpkb	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
	+-						
	lpkb						
	L1.	0083797	.0155322	-0.54	0.591	0394184	.022659
	1						
	pop	-1.948416	1.101845	-1.77	0.082	-4.150278	.2534458
•	ki	.0044077	.0011992	3.68	0.000	.0020112	.0068042
•	_cons	.2666348	.178572	1.49	0.140	0902129	.6234824

Cross section 2000-2005

. reg dpkb l.lpkb pop ki if num5==12

•	Source	SS	df	MS		Number of obs	= 188
•	+-					F( 3, 184)	= 3.32
•	Model	.173363788	3.0.	57787929		Prob > F	= 0.0211
•	Residual	3.20406699	184 .0	17413408		R-squared	= 0.0513
•	+-					Adj R-squared	= 0.0359
•	Total	3.37743078	187 .0	18061127		Root MSE	= .13196
•							
•	dpkb	Coef.	Std. Err	. t	P> t	[95% Conf.	Interval]
•	+-						
•	lpkb						
•	L1.	002166	.0096033	-0.23	0.822	0211127	.0167806
•	-						
•	pop	-2.365138	.9445526	-2.50	0.013	-4.228684	5015923
•	ki	.0005987	.0007476	0.80	0.424	0008762	.0020736
•	_cons	.3326403	.138821	2.40	0.018	.0587548	.6065258
•							

## Pooled regression for every cross section:

• . reg dpkb l.lpkb pop ki

	Source	SS	df	MS		Number of obs	=	1590
	+					F( 3, 1586)	=	46.18
	Model	3.6690368	3 1	L.22301227		Prob > F	=	0.0000
	Residual	42.0022271	1586 .	.026483119		R-squared	=	0.0803
	+					Adj R-squared	=	0.0786
	Total	45.6712639	1589 .	.028742142		Root MSE	=	.16274
•	dpkb	Coef.	Std. Er	rr. t	P> t	[95% Conf.	Int	terval]
•	+							
•	lpkb							
•	L1.	0124278	.004002	-3.11	0.002	0202781	(	0045776
•								
•	pop	-1.427988	.325293	-4.39	0.000	-2.066039	'	7899376
•	ki	.0033681	.000347	79 9.68	0.000	.0026856	. (	0040505
•	_cons	.2498058	.049747	71 5.02	0.000	.1522287	• •	3473828
•								

## Error clustering? Double the errors.

regdpkbl.lpkbpop ki, vce(cluster cty)

Number of obs	=	1590
F( 3, 187)	=	13.69
Prob > F	=	0.0000
R-squared	=	0.0803
Root MSE	=	.16274

(Std. Err. adjusted for 188 clusters in cty)

	1		Robust				
dpkb	I	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
	-+-						
lpkb	1						
L1.	I	0124278	.0062808	-1.98	0.049	0248182	0000374
	1						
pop	I	-1.427988	.6651244	-2.15	0.033	-2.7401	1158769
ki	I	.0033681	.000809	4.16	0.000	.0017721	.004964
_cons	1	.2498058	.0965514	2.59	0.010	.0593357	.4402758

Linear regression

Error clustering? Double the errors.

- Estimating the model with OLS yields biased results because the estimator is inconsistent.
- There are unobservable constant effects for countries (factors constant over time, not included in the model), which causes the dependent variable to change faster for some observation units than others.

# $E\left[x_{it}'(\eta_i + \nu_i)\right] \neq 0$

Panel data estimators

- Why cross-sectional-time estimators?
- Panel data allow to analyze the phenomenon simultaneously in time and in cross-section or spatial dimensions. These estimators allow to isolate the individual specificity of individual objects.
- The use of data panels allows for greater heterogeneity (greater diversity) of study units.
- Provides more degrees of freedom and increases the efficiency of estimation.
- Extracting periodic effects makes it easier to study the dynamics of adjustment.
- Panel data allows you to isolate the influence of unobservable variables or effects.

## Panel data estimation

Standard panel:

$$\Delta y_{it} = \gamma_t + (\alpha - 1)y_{i,t-1} + \sum_{j=1}^k \beta_j x_{itj} + \varepsilon_{it} \text{ dla } i = 1, ..., N \text{ i } t = 1, ..., T.$$

$$\varepsilon_{it} = \eta_i + \gamma_{it} + v_{it}$$

Panel estimators are more efficient over OLS because they use unused information – the panel dimension. Fixed Effects, Between Effects, Random Effects global xlist l.lpkb pop ki quietly regress dpkb \$xlist, vce(cluster cty) estimates store OLS quietly xtreg dpkb \$xlist, be estimates store BE quietly xtreg dpkb \$xlist, re vce(robust) estimates store RE quietly xtreg dpkb \$xlist, fe vce(robust) estimates store FE

Hausmann test hausman fe re Strong fixed effect! xtreg dpkbl.lpkb pop ki, fe

One way or two way? Wald test

xtregar dpkb l.lpkb pop ki, fe rhotype(dw) lbi xi: xtregar dpkb l.lpkb pop ki i.num5, fe rhotype(dw) lbi

test ( \_Inum5\_3 \_Inum5\_4 \_Inum5\_5 \_Inum5\_6 \_Inum5\_7
\_Inum5\_8 \_Inum5\_9 \_Inum5\_10 \_Inum5\_11 \_Inum5\_12 \_Inum5\_2)

NOTE ON THE TWO WAY MODEL IN MACROECONOMICS

# **ALGORITHM**

- ▶ 1. Panel>MNK, very rare if not.
- > 2. FE versus RE, BE Hausmann test. Very rare if not FE.
- ▶ 3. Determine whether one or two-way model.

- Nickell (1981) In FE there is still a correlation between the lagged dependent variable and the transformed error expression, which makes these estimators have the desired properties purely asymptotically, i.e. when the number of observations over time tends to infinity.
- This is not the case of a typical growth model where usually there are significantly less than 50 observations over time (due to averaging, it is usually 5-10 observations).

- By definition, this method limits the analysis to looking for the mean within countries, perhaps ignoring significant differences between countries.
  - This method does not help in any way to solve the problem of causality, measurement error and omitted variables, variables over time.
  - It also does not allow for estimating the impact of variables that are constant over time, such as the impact of geography or history, on economic growth.

# Let us move forward

#### **Estimators:**

- Anderson-Hsiao,
- Arellano-Bond,
- Blundell-Bonda,
- ► PMG,
- Kiviet's.

# Differencing

 $\Delta y_{it} = \alpha \Delta y_{i,t-1} + \Delta \mathbf{x}_{it} \boldsymbol{\beta} + \Delta \boldsymbol{\varepsilon}_{it}$ 

- •Getting rid of fixed effect, not much else.
- •This transformation uses  $y_{i,t-1}$  and therefor causes endogeneity, because

 $y_{i,t-1}$  in  $\Delta y_{i,t-1} = y_{i,t-1} - y_{i,t-2}$  is correlated with  $\varepsilon_{i,t-1}$  in  $\Delta \varepsilon_{it} = \varepsilon_{it} - \varepsilon_{i,t-1}$ 

 However, if there is no autocorrelation, the lagged variables may be exogenous, they may be used as instruments.

# One option: 2SLS (Anderson i Hsiao 1981)

- After differentiating the fixed effects, a natural estimator of the Instrumental Variable Method is available.
- We can construct instruments from the lagged dependent variable, lagged twice, three times, etc.
- The solution to the problem of measurement error and opposite causality is the 2SLS estimator by Anderson and Hsiao (1981)
- It assumes estimating the model on the first differences and using the past GDP level in the second lag as an instrument for lagging first GDP differences.

# 2SLS (Anderson i Hsiao 1981)

- Assuming the absence of AR () in  $\mathcal{E}_{it}$ , natural instruments for  $\Delta y_{i,t-1}$  are  $\Delta y_{i,t-2}$  and  $y_{i,t-2}$
- Very close to  $\Delta y_{i,t-1}$ . Maybe collinearity?
- $y_{i,t-2}$  is more sensible: starting from t = 3
- Nevertheless, we lose a lot of observation when T is small.
- Similarly, for other variables

# 2SLS (Anderson i Hsiao 1981)

ssc install xtivreg28
xi: xtivreg2 dpkb pop lki i.num5 (lpkb
= l.lpkb), fd
help xtivreg2

IV (2SLS) estimation								
Estimates efficient for homoskedasticity only Statistics consistent for homoskedasticity only [del]								
D.dpkb   Coef. Std. Err. z P> z  [95% Conf.								
lpkb   D1.   -1.590232 .1577865 -10.08 0.000 -1.899488								
[del] Underidentification test (Anderson canon. corr. LM statistic): 225.987 Chi-sq(1) P-val = 0.0000								
Weak identification test (Cragg-Donald Wald F statistic):266.985Stock-Yogo weak ID test critical values:10% maximal IV size16.3815% maximal IV size8.9620% maximal IV size6.66								
25% maximal IV size 5.53 Source: Stock-Yogo (2005). Reproduced by permission.								
Sargan statistic (overidentification test of all instruments): 0.000 (equation exactly identified)								

# 2SLS (Anderson i Hsiao 1981)

- Assuming the absence of AR () in  $\mathcal{E}_{it}$ , natural instruments for  $\Delta y_{i,t-1}$  are  $\Delta y_{i,t-2}$  and  $y_{i,t-2}$
- Very close to  $\Delta y_{i,t-1}$ . Maybe collinearity?
- $y_{i,t-2}$  is more sensible: starting from t = 3
- Nevertheless, we lose a lot of observation when T is small.
- Similarly, for other variables

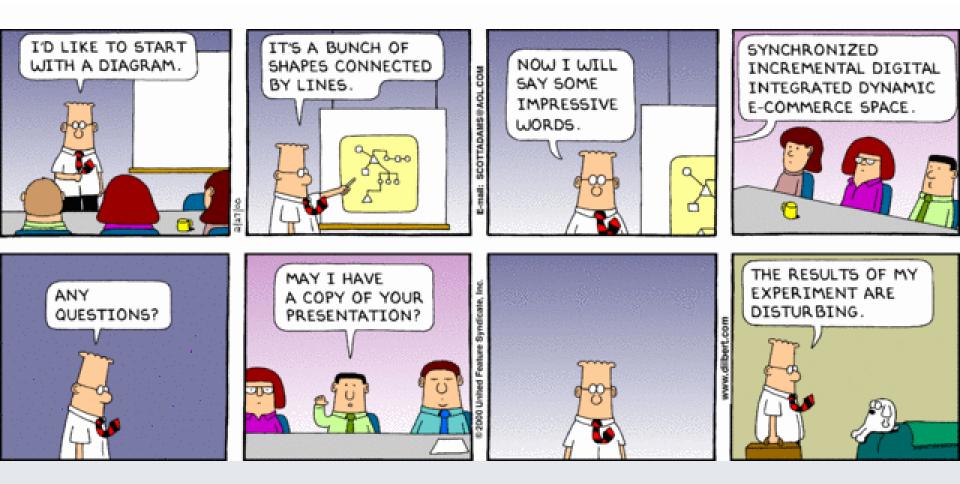
# One option: 2SLS (Anderson i Hsiao 1981)

It allows to isolate the part of the dependent variable variation that is not related to the opposite causality, omitted variables and the measurement error.

This method leads to consistent estimates, but they may be ineffective when the random term is nonspherical due to the lack of use of all moment conditions (Hansen, 1982).

# One option: 2SLS (Anderson i Hsiao 1981)

- Need for further lags undesirable as it: o Reduces T.
  - o Problem with short panels
  - After differentiation, errors not i.i.d.
  - o differences in errors correlated
  - o 2SLS ineffective



# Hansen (1982)

The sensibility of introducing an instrument in the form of a lag of the dependent variable can be written in the form of an moment identifying assumption:

$$E\left[\left(u_{it}-u_{i,t-1}\right)y_{i,t-2}\right]$$

To increase the efficiency of the estimator, Arellano and Bond (1991) use all possible instruments in the form of lags and differences.

The sensibility of introducing these instruments should be written in the form of conditions related to moments, identifying assumptions that are used to build the estimator of the Generalized Method of Moments.



Solution: IV & GMM instruments (Holtz-Eakin, Newey, and Rosen 1988)

- •Use of a lot of lags. In the absence, use zero in the matrix.
- Instruments for each delay and period have been created.

$$\begin{bmatrix} \cdot \\ \cdot \\ y_{i1} \\ \vdots \\ y_{i,T-2} \end{bmatrix} \text{GMM:} \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & \cdots \\ 0 & 0 & 0 & 0 & 0 & 0 & \cdots \\ y_{i1} & 0 & 0 & 0 & 0 & 0 & \cdots \\ 0 & y_{i2} & y_{i1} & 0 & 0 & 0 & \cdots \\ 0 & 0 & 0 & y_{i3} & y_{i2} & y_{i1} & \cdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \ddots \end{bmatrix}$$

•Result: Arellano-Bond (1991) difference GMM

#### Solution: IV & GMM instruments (Holtz-Eakin, Newey, and Rosen 1988)

The moment conditions were created with the assumption that the lagged levels of the dependent variable are orthogonal to the differentiated shock are known as GMM moment conditions.

The moment conditions created using strictly exogenous variables are simply the standard conditions of the instrumental variables (IV) method, they are also called standard moment conditions.

#### Solution: IV & GMM instruments

- Number of instruments:
- ▶ p = T − 2 (one period for differences, one for lagged difference)
- ▶ k + p \* (p + 1)/2
- Where k is the number of exogenous variables.

#### xtabond dpkb l.lpkb pop ki, lags(1) vce(robust) artests(2)

►	Arellano-Bond dynamic panel	ation 1	Number of	= 1214					
•	Group variable: cty	1	Number of	groups =	= 188				
•	Time variable: num5								
•			(	Obs per gr	oup: min =	= 1			
					avg =	6.457447			
►					max =	= 9			
	Number of instruments =	49	Ĺ	Wald chi2(	= 233.09				
•			I	Prob > chi2 = 0.0000					
•	One-step results								
•		(S	td. Err	. adjusted	for cluster	ing on cty)			
•									
		Robust							
•	dpkb   Coef.				[95% Conf.	. Interval]			
•	·								
	dpkb   L1.  1297861	0407782	_3 10	0 001	- 20971	- 0108623			
	LI.  1297001	.0407782	-3.10	0.001	20971	0498023			
	lpkb								
	L1.  2716851	.0271594	-10.00	0.000	3249166	2184536			
•			20000						
•	pop   -2.914595	1.661945	-1.75	0.079	-6.171947	.3427576			
•	ki   .0057089								
•	_cons   2.534362	.2645364	9.58	0.000	2.01588	3.052844			
►									
•	Instruments for differenced	equation							
•	GMM-type: L(2/.).dpkb								
•	Standard: LD.lpkb D.pop D.ki								
•	Instruments for level equat	ion							

#### Solution: IV & GMM instruments

- Number of instruments:
- ▶ p = 12 3
- 4 + 9 \* (9 + 1)/2
- ► =49

# Problem: the errors appear too small

	(1) step	(2) step
L.dpkb	-0.0784** (-3.16)	-0.118*** (-4.50)
L2.dpkb	-0.176*** (-7.27)	-0.112*** (-6.41)
L.lpkb	-0.443*** (-25.45)	-0.444*** (-19.57)
рор	-0.358 (-0.63)	-1.103 (-1.84)
ki	0.00468*** (5.77)	0.00538*** (6.05)
cons	3.734*** (23.94)	3.789*** (19.93)
N	1026	1026

#### Problem, cont'd

- Problem appears to be one of overfitting

   Efficient GMM deemphasizes moments
   with high variance (high second moments)
   Feasible efficient GMM in small samples
   may deemphasize outliers (high first
   moments)
  - Spurious precision

#### **Problem: finite sample**

Let us compare:

- xi: xtabond dpkb l.lpkb pop ki i.num5, lags(2)
- eststo AB ONESTEP
- xi: xtabond dpkb l.lpkb pop ki i.num5, lags(2) two
- eststo AB\_TWOSTEP
- xi: xtabond dpkb l.lpkb pop ki i.num5,
  lags(2) two
- eststo AB\_TWOSTEP\_WIND
- esttab

#### Solution Windmeijer correction (2005)

Oszacowanie 1-stopniowe:  $\hat{\beta}_1 = f(\mathbf{Y})$ (warunkowo względem **X**, **Z**)

Oszacowanie 1-stopniowe błędów do  $\hat{\Omega}$ :

$$\hat{\boldsymbol{\beta}}_{2} = \left(\mathbf{X}'\mathbf{Z}\left(\mathbf{Z}'\hat{\boldsymbol{\Omega}}\mathbf{Z}\right)^{-1}\mathbf{Z}'\mathbf{X}\right)^{-1}\mathbf{X}'\mathbf{Z}\left(\mathbf{Z}'\hat{\boldsymbol{\Omega}}\mathbf{Z}\right)^{-1}\mathbf{Z}'\mathbf{Y} \equiv g(\mathbf{Y},\hat{\boldsymbol{\Omega}}) \equiv g(\mathbf{Y},f(\mathbf{Y}))$$

Standardowe oszacowanie  $\operatorname{Var}[\hat{\beta}_2]$  uznaje  $\hat{\Omega}$  za stałą, obserwowaną i dokładną – pomimo zależności od losowego **Y** Roszerzenie Taylora *g* wokół prawdziwego  $\beta$ :

$$\hat{\boldsymbol{\beta}}_{2} = g\left(\mathbf{Y}, \hat{\boldsymbol{\Omega}}_{\hat{\beta}_{1}}\right) \approx g\left(\mathbf{Y}, \hat{\boldsymbol{\Omega}}_{\beta}\right) + \frac{\partial}{\partial \hat{\boldsymbol{\beta}}} g\left(\mathbf{Y}, \hat{\boldsymbol{\Omega}}_{\hat{\beta}}\right) \Big|_{\hat{\boldsymbol{\beta}}=\boldsymbol{\beta}} \left(\hat{\boldsymbol{\beta}}_{1} - \boldsymbol{\beta}\right)$$

"Korekta" bierze się z drugiego wyrazu:  $E[\hat{\beta}_1 - \beta] = 0$  zatem  $E[\hat{\beta}_2]$ —brak obciążeń współczynników Wpływ jedynie na błędy.

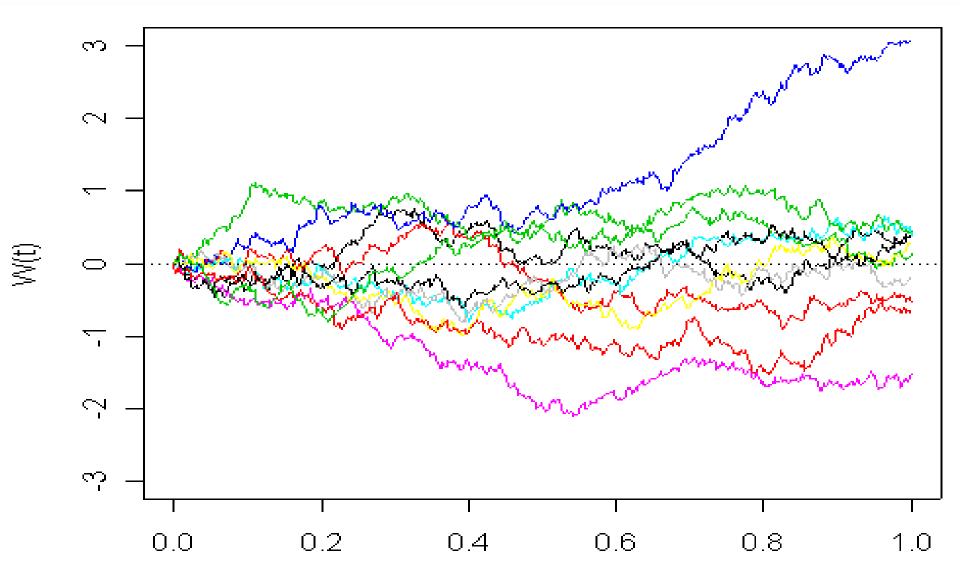
(1)	(2)	(3)	
	ONESTEP	TWOSTEP	TWOSTEP_WIND
L.dpkb	-0.0784**	-0.118***	-0.118*
	(-3.16)	(-4.50)	(-2.18)
L2.dpkb	-0.176***	-0.112***	-0.112***
	(-7.27)	(-6.41)	(-3.41)
L.lpkb	-0.443***	-0.444***	-0.444***
	(-25.45)	(-19.57)	(-10.65)
pop	-0.358	-1.103	-1.103
	(-0.63)	(-1.84)	(-0.70)
ki	0.00468***	0.00538***	0.00538***
	(5.77)	(6.05)	(3.66)
_cons	3.734***	3.789***	3.789***
	(23.94)	(19.93)	(11.23)
Ν	1026	1026	1026
t statistics	s in parentheses		
* ~~~ 0 05 **	k = n < 0 = 0 = 1 + k + k = n < 0 = 0	0.1	

\* p<0.05, \*\* p<0.01, \*\*\* p<0.001</pre>

# **Problem: Weak instruments**

If *y* is nearly a random walk,  $y_{i,t-1}$  is a poor instrument for  $\Delta y_{it}$ , mathematical relationship notwithstanding

# **10 Random Walks**



## **Problem: weak instruments**

- . sort cty num5
- . correlate lpkb L.lpkb L2.lpkb L3.lpkb L4.lpkb L5.lpkb L6.lpkb

1		L.	L2.	L3.	L4.	L5.	L6.
	lpkb +	lpkb	lpkb	lpkb	lpkb	lpkb	lpkb
lpkb							
	1.0000						
L1.	0.9926	1.0000					
L2.	0.9770	0.9920	1.0000				
L3.	0.9559	0.9730	0.9894	1.0000			
L4.	0.9311	0.9500	0.9686	0.9878	1.0000		
L5.	0.8989	0.9201	0.9409	0.9650	0.9881	1.0000	
L6.	0.8680	0.8897	0.9123	0.9391	0.9668	0.9881	1.0000

Solution: Instead of purging fixed effects, find instruments orthogonal to them (Arellano and Bover 1995)

- If  $E[y_{it} \mu_i]$  stationary, then  $E[\Delta y_{it} \mu_i] = 0$
- $\Delta y_{i,t-1}$  uncorrelated with fixed effects, thus with  $v_{it} = \mu$  good instrument in *levels* (if no AR)
- Make system of difference and levels equations
- Concretely, make a stacked data set, with differenc up top, levels below. Treat as single estimation pro
- Instrument differences with levels and v.v.

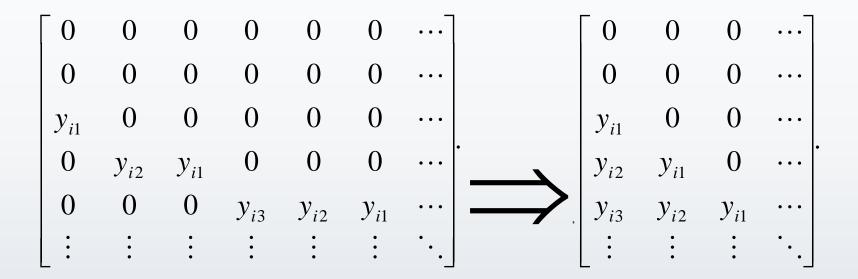
• "System GMM" (Blundell and Bond 1998)

#### Problem: too many instruments

- In difference and system GMM, # instruments (*j*) quadratic in *T*
- Analogy:
  - In 2SLS, if j = # of regressors, first-stage R2's=1.0 and 2SLS=OLS (biased)
  - Too many instruments overfit endogenous variables
- And # of cross-moments in  $\operatorname{Var}[\mathbf{Z}'\mathbf{E}|\mathbf{X},\mathbf{Z}]^{-1}$  to be estimated for efficient GMM quadratic in *j*—quartic in *T*!
- Estimate of  $\operatorname{Var}[\mathbf{Z}'\mathbf{E}|\mathbf{X},\mathbf{Z}]^{-1}$  degrades
- Hansen test very weak—p values of 1.000 not uncommon
- Little guidance on how many is too many
- xtabond2 warns if j > N

#### Solution: consider limiting instruments

Limit number of lags of variables used as instrumentsOr "collapse" instruments:



$$\sum_{i} y_{i,t-2} \Delta \hat{e}_{it} = 0 \text{ for each } t \ge 3$$

$$\sum_{i,t} y_{i,t-2} \Delta e_{it} = 0.$$

# Arellano-Bond AR() test

- Expect AR() in  $V_{it} = \mu_i + \varepsilon_{it}$
- To check for AR(1) in  $\mathcal{E}_{it}$ , test for AR(2) in  $\Delta e_{it}$
- E.g., compare  $e_{it} e_{i,t-1}$  and  $e_{i,t-2} e_{i,t-3}$  to detect  $e_{i,t-1} \sim e_{i,t-2}$
- Test statistic for AR(*l*) in differences:  $\sum_{i,t} \Delta e_{it} \Delta e_{i,t-l}$
- Normal under null of no AR(*l*)
- Arellano and Bond calculate its standard deviation
- z test for AR()
- More general than other AR() tests in Stata.
- abar: post-estimation command for regress, ivreg, ivreg2
- •estat abond



#### xtunitroot fisher lpkb, dfuller lags(0)

Fisher-type unit-root test for lpkb Based on augmented Dickey-Fuller tests								
Ho: All panels contain uni	t roots	Number of panels = 190						
Ha: At least one panel is	station	ary	Avg. number of periods = $9.37$					
AR parameter: Panel-specific Asymptotics: T -> Infinity Panel means: Included Time trend: Not included								
Drift term: Not included		ADF regressions: 0 lags						
		Statistic	p-value	_				
Inverse chi-squared(376)	P	680.9705	0.0000					
Inverse normal	Z	2.6933	0.9965					
Inverse logit t(924)	L*	-0.8559	0.1962					
Modified inv. chi-squared	Pm	11.1211	0.0000					

P statistic requires number of panels to be finite.

Other statistics are suitable for finite or infinite number of panels.

 Blundell and Bond (1998) proposed to use, in addition to regression on differences, additional regression at levels with delayed variables as instruments. This requires the fulfillment of additional momentum conditions that are based on stationarity conditions relative to the initial observation:

$$E\left[\Delta y_{i,t-s} \left( (\eta_i + v_{it}) \right) \right] = 0$$

These conditions are met when the data generation process is mean-stationary:

$$y_{i,1} \frac{n_i}{(1-\alpha)} + \varepsilon_i \operatorname{przy} E(\varepsilon_i) = E(\varepsilon_i \eta_i) = 0$$

$$x_{i,1} \frac{n_i}{(1-\alpha)} + \varepsilon_i \text{ przy } E(\varepsilon_i) = E(\varepsilon_i \eta_i) = 0$$

Blundell and Bond (2000) show that this condition is not really a necessary condition. Considering the equation in the first, it can be shown that if:

$$E(\eta_i \, \Delta x_{i,t}) = 0$$

and assuming that the same data generation process resulted in GDP per capita data in a given data series in the sample for a sufficiently long period before the selected sample, that the impact of the baseline conditions (in this case, the initial capital level) can be considered negligible, then:

$$E(\eta_i \, \Delta y_{i,t}) = 0$$

- It can be seen that if the first differences of these variables were correlated with the fixed effects for a given country, it would have incredible long-term implications.
  - This does not mean that, for a given country, the constant effects do not play any role in determining growth. Their influence is one of the determinants of the steady state of the production level per unit of labor productivity, depending on other conditions in the steady state. The essence of these assumptions is that there is no correlation between the increase in production and the fixed effect, with no control for the presence of other variables.

As shown in Monte Carlo simulations (e.g. (Blundell and Bond, 1998, Blundell, et al. 2000), when these conditions are met, the resulting UMM estimator on differences and levels (hereinafter BB, the GMM System) has better finite load and RMSE properties than Arelllano and Bond's differential estimator.

## Problem: heteroscedastisity & AR

 In the presence of heteroscedasticity and autocorrelation in the model, it is possible to use a two-stage UMM estimator using the first step (Davidson and MacKinnon, 2004) to estimate the residual weight matrix of the estimate.
 We want it to be directly proportional to the inverse of the variance and covariance matrices of the instruments, i.e. the matrix:

$$V\left\{Z_{i} \Delta \varepsilon_{i}\right\} = E\left\{Z_{i} \Delta \varepsilon_{i} \Delta \varepsilon_{i} Z_{i}\right\}$$
$$p \lim_{N \to \infty} W_{N} = E\left\{Z_{i} \Delta \varepsilon_{i} \Delta \varepsilon_{i} Z_{i}\right\}^{-1}$$

# Problem: heteroscedastisity & AR

Using the mean:

$$\hat{\mathbf{W}}_{N}^{opt} = \left(\frac{1}{N}\sum_{i=1}^{N}\mathbf{Z}_{i}'\Delta\hat{\boldsymbol{\epsilon}}_{i}\Delta\hat{\boldsymbol{\epsilon}}_{i}'\mathbf{Z}_{i}\right)^{-1}$$

However, there are no estimates of the residual values.
 Solution: the two-step method.

# Solution: two-step procedure

- The model is estimated using the instrumental variable method by substituting the unit matrix for the WN matrix, obtaining estimates of the residuals
   The obtained estimator is unbiased and consistent, but it is not effective because the selected matrix is not optimal
- We use the obtained estimates of the error term from the first step to estimate the optimal WN matrix, which we then use in the second step to estimate the final parameters.

## Solution: two-step procedure

While asymptotically more efficient, the two-stage GMM estimator in finite samples provides estimates of standard errors that are heavily biased downwards. It is possible to solve this problem by means of a twostep covariance correction in a finite sample proposed by Windmeijer (2005). This adjustment makes the robust two-stage GMM estimator on differences and levels more effective than the robust one-stage estimators, even when the panel is relatively short (correction already discussed in the context of the AB estimator)

### Problem: measurement error and causality

- Additionally, the estimator solves the problem of measurement error and opposite causality. Bond et al. (2001) indicate that thanks to the use of binary variables corresponding to successive time periods, the time-varying measurement error in a given observed series in the sample will have no consequences for the model estimation and this does not affect the validity of the GMM instruments used.
  - In turn, lags in levels help reduce the problem of opposite causality.

The coefficient thus estimated takes into account Granger causality.



# **Problem: exogeneity**

In the methods presented so far, endogenous instruments are used. For example, in the case of GMM levels and differences in empirical models, most often in the equation of the first differences in growth, the differences of the explanatory variables and the second lags in the level of the dependent variable are used, and in the case of the equation of levels, these are the delayed first differences of the dependent variable.

It is possible to include exogenous instrumental variables in the model, which allows for taking into account variables that may have the opposite causality, or to act as a third variable. xtdpdsys dpkb l.lpkb pop ki, lags(1) vce(robust) artests(2)

•	System dynamic	Ν	Number of obs = 1402					
•	Group variable	Ν	Number of groups			188		
•	Time variable:	num5						
•				0	Obs per group:			2
•							avg =	7.457447
•							max =	10
•	Number of inst	ruments =	58	W	ald chi2(	4)	=	119.68
•				Prob > chi2 =			0.0000	
•	One-step resul	ts						
•								
•	I		Robust					
	dpkb	Coef.	Std. Err.	Z	P> z	[95%	Conf.	Interval]
•	+							
•	dpkb							
•	L1.	.0397641	.0395016	1.01	0.314	0376	5575	.1171858
•	1							
•	lpkb							
•	L1.	2473419	.0269692	-9.17	0.000	3002	2005	1944833
•	1							
•	pop	-3.494342	2.070097	-1.69	0.091	-7.551	657	.5629743
•	ki	.0047215	.0012743	3.71	0.000	.0022	239	.0072191
+	_cons	2.386552	.3516864	6.79	0.000	1.697	259	3.075844
+								
	Instruments fo	r differenced	d equation					
	GMM-ty	pe: 1.dr	okb					

- > estat abond
- > artests not computed for one-step system estimator with
  vce(gmm)
- Arellano-Bond test for zero autocorrelation in firstdifferenced errors
- +----+
- > |Order | z Prob > z|
- I ----- |
- ▶ | 1 |-4.7181 0.0000 |
- | 2 |-2.1149 0.0344 |
   +-----+
- H0: no autocorrelation

> estat sargan

Also problems. To solve the problem proceed with the same operation as xtabond, we increase the lags parameter, we switch to the two-step method.

Own exercises - come to the correct form of the Blundell-Bond model analogically to Arellano-Bond. Let me just hint that it will be easier with dummy variables.

### Problem: sooo, BB or AB?

- Additional conditions for the BB estimator can be tested with the differential Sargan test known as the Hansen C test or J test.
  - The easiest way to download the xtabond2 module:
- > net install xtabond2
- And repeat the estimates using this module. Syntax available on:
- Roodman (2006) How to do xtabond2

# Problem: small N size

This is often the case for research of a regional nature. The estimator proposed by Kiviets (1995), which considers the correction of the model of the first differences in a balanced panel, where the number N is necessarily small.

#### Problem: small N size

This creates a revised estimate of the fixed effects that is more effective than the estimates of Anderson and Hsiao (1981), Arellano and Bond (1995) and Blundell and Bond (1998) with small T and N. Bruno (2005) presents a modified version of this estimator for unbalanced panels, which is important in the case of growth models, when the length of the time series is different for different countries.

#### Problem: small N size

The disadvantage of this methodology is the assumption of the strict exogeneity of the explanatory variables and the inability to take into account the opposite causality and measurement error, which undermines the use of this estimator in dynamic growth models in applications other than small (regional) country samples. Installation of the Kiviets estimator in Bruno's version (2005): net install xtlsdvc

The need to install an additional package for the GMM System: net install xtabond2

Syntax

xtlsdvc lpkb pop ki, initial (bb) vcov(50)

#### The effective estimator in the parentheses:

- Bb Blundell bond
- AB Arellano Bond
- FD Anderson Hsiao

#### xtlsdvc lpkb pop ki, initial (bb)

LSDVC dynamic regression (SE not computed)						
lı Conf. Ir	-	Coef.	Std. Err.	Z	₽> z	[95%
-	+ pkb   L1.	.9631341	·	··	·	
ł		.6083637	•	•	•	
•	· ki	.0051197	•	•		

 Another problem raised in the econometric literature on growth estimation is the heterogeneity of countries. Until now, it was assumed that for all countries the estimated coefficients are the same, and therefore for each j and i:

$$\beta_{ij} = \beta_j$$

 Is it so? Are all objects from the same distribution?
 If we increase the period of education by one year, will the effect be the same in Japan, Poland and Burkina Faso?

 This type of problem cannot be solved with country samples. There are too few of them. Nevertheless, one can move towards methods with heterogeneous coefficients. Condition: N> 500.
 However, it is possible to solve the heterogeneity between short-run factors, assuming that in the long-

run case they are converging the same CE.

The Pooled Mean Group (PMG) estimator when applied to estimating economic growth can be described by the following equation :

$$\Delta y_{i,t} = \sum_{z=1}^{p-1} \gamma_i \Delta y_{i,t-z} + \sum_{z=0}^{q} \tau_i \Delta x_{i,t-z} + \varphi_i \left( y_{i,t-1} - \alpha_i - \sum_{j=1}^{k} \beta_j x_{i,j,t-1} \right) + \varepsilon_{i,t}.$$

This equation makes it possible to separately estimate the short-term dynamics of the explained variable and the long-term dynamics, thanks to the inclusion of a cross-sectional time error correction mechanism in the sample, different for different countries.

#### net install xtpmg xtpmg dpkb d.lpop d.lki, lr(l.lpkb lki lpop) pmg

Pooled Mean Group Regression: Estimated Error Correction Form (Estimate results saved as PMG)							
		Coef.				[95% Conf.	Interval]
ec	+						
	ki	.0505416	.0078991	6.40	0.000	.0350597	.0660235
		-8.557502				-19.0973	1.9823
SR							
	ec	1009378	.0101466	-9.95	0.000	1208248	0810508
	pop						
	D1.	1.161559	.4925535	2.36	0.018	.1961723	2.126947
	ki						
	D1.	.0007548	.0007747	0.97	0.330	0007636	.0022732
		.9078603	.1079748	8.41	0.000	.6962335	1.119487

Ok. all the most common methods are discussed. It remains to be discussed what is less frequently used in economics due to the short panel problems.
 xtrc - allows you to estimate with the assumption of variable coefficients. This corresponds to a different coefficient for each country for each variable.
 xtmixed - hierarchical models.
 So far linear models. There are also extensions of

nonlinear models to panels.

### Zakończenie

Model	Przekształcenie danych	Zmienne objaśniające	Zgodność
FE	Wewnątrzobiektowe	$y_{i,t-1}, x_{i,t}$	nie
FEDW	Wewnątrzobiektowe	$y_{i,t-1}, x_{i,t}$	tak
AH	$\Delta$	$\Delta y_{i,t-1}, \Delta x_{i,t}$	tak
AB	$\Delta$	$\Delta y_{i,t-1}, \Delta x_{i,t}$	tak
BB	$\Delta$	$\Delta y_{i,t-1}, \Delta x_{i,t}, y_{i,t-1}, x_{i,t}$	tak
Kiviets	$\Delta$	$\Delta y_{i,t-1}, \Delta x_{i,t}, y_{i,t-1}, x_{i,t}$	tak
PMG	$\Delta$	$\Delta y_{i,t-1}, \Delta x_{i,t}, y_{i,t-1}, x_{i,t}, ECM$	tak

- 1. Panel>MNK, very rare if not.
- 2. FE versus RE, BE Hausmann test. Very rare if not FE.
- 3. Determine whether one or two-way model.

- 4. Anderson-Hsiao, Craigg-Donald whether instruments exogenous on the first stage.
- 5. Arellano-Bond one or two step Sargan test & Arellano-Bond AR test.
- 6. If the tests are pointing to problems, increase the number of instruments, switching from the one-stage method to the two-stage method, increasing the number of instruments.

- 7. Blundell Bond as with Arellano Bond, but J-Hansen test to see whether additional GMM-sys constraints are viable.
  - If not & small N size Kiviet's
  - If not & heterogeneity, long T PMG.
- If you choose Kiviet's or PMG it is nice to show robustness! You can always run the Hausman test against the FE!

 The biggest problem of empirical research in macroeconomics is the uncertainty of model parameters and explanatory variables.
 Trivializing - what's on the right?

### Last but not least problems

Outliers, missing data?

Many tests for outliers:

net install grubbs

But first, it's best to draw figures like in the first class and see if any observations are exceptionally different. Missing data:

- > ipolate
- > epolate



# Dziękuję za uwagę.