## Vicroeconomics

## Lecture 2

## Quantity Taxes

- A quantity tax levied at a rate of $\$ t$ is a tax of $\$ t$ paid on each unit traded.
- If the tax is levied on sellers then it is an excise tax.
- If the tax is levied on buyers then it is a sales tax.


## Quantity Taxes

- A tax rate $t$ makes the price paid by buyers, $p_{b}$, higher by $t$ from the price received by sellers, $p_{s}$,

$$
p_{b}=p_{s}+t
$$

## Quantity Taxes

- Even with a tax the market must clear.
- l.e. quantity demanded by buyers at price $p_{b}$ must equal quantity supplied by sellers at price $p_{s}$

$$
D\left(p_{b}\right)=S\left(p_{s}\right)
$$

## Quantity Taxes

$p_{b}=p_{s}+t$ and $D\left(p_{b}\right)=S\left(p_{s}\right)$ describe the market's equilibrium.

Notice these conditions apply no matter if the tax is levied on sellers or on buyers.

Hence, a sales tax rate $\$ t$ has the same effect as an excise tax rate $\$ t$.

## Quantity Taxes \& Market Equilibrium



And sellers receive only $p_{s}=p_{b}-t$.

## Quantity Taxes \& Market Equilibrium



And buyers pay $p_{b}=p_{s}+t$.

## Quantity Taxes \& Market Equilibrium

| Market | Market <br> supply |
| :--- | :--- | :--- | :--- |
| A sales tax levied at |  |

## Quantity Taxes \& Market Equilibrium



## Quantity Taxes \& Market Equilibrium

-E.g. suppose the market demand and supply curves are linear,

$$
\begin{aligned}
& D\left(p_{b}\right)=a-b p_{b} \\
& S\left(p_{s}\right)=c+d p_{s^{\prime}}
\end{aligned}
$$

Quantity Taxes \& Market Equilibrium $D\left(p_{b}\right)=a-b p_{b}$ and $S\left(p_{s}\right)=c+d p_{s}$.
With the tax, the market equilibrium satisfies

$$
\begin{aligned}
& p_{b}=p_{s}+t \text { and } D\left(p_{b}\right)=S\left(p_{s}\right) \text { so } \\
& p_{b}=p_{s}+t \text { and } a-b p_{b}=c+d p_{s^{\prime}}
\end{aligned}
$$

Substituting for $p_{b}$ gives

$$
a-b\left(p_{s}+t\right)=c+d p_{s} \Rightarrow p_{s}=\frac{a-c-b t}{b+d}
$$

## Quantity Taxes \& Market Equilibrium

$$
p_{s}=\frac{a-c-b t}{b+d} \text { and } p_{b}=p_{s}+t \text { give }
$$

$$
p_{b}=\frac{a-c+d t}{b+d}
$$

The quantity traded at equilibrium is

$$
\begin{aligned}
q^{t} & =D\left(p_{b}\right)=S\left(p_{s}\right) \\
& =a+b p_{b}=\frac{a d+b c-b d t}{b+d}
\end{aligned}
$$

As $t$ increases,
$p_{s}$ and $q^{t}$ falls, $p_{b}$ rises

## Quantity Taxes \& Market Equilibrium

The total tax paid (by buyers and sellers combined) is

$$
T=t q^{t}=t \frac{a d+b c-b d t}{b+d} .
$$

The tax paid per unit by the buyer is

$$
p_{b}-p^{*}=\frac{a-c+d t}{b+d}-\frac{a-c}{b+d}=\frac{d t}{b+d} .
$$

The tax paid per unit by the seller is

$$
p^{*}-p_{s}=\frac{a-c}{b+d}-\frac{a-c-b t}{b+d}=\frac{b t}{b+d} .
$$

# Tax Incidence and Own-Price Elasticities 

- The tax incidence of a buyer and a seller indicates what is the unit tax paid by the buyer relative to the unit tax paid by the seller, $\left(p_{b}-p^{*}\right) /\left(p^{*}-p_{s}\right)$.


## Tax Incidence and Own-Price Elasticities

- In case of linear demand and supply curves the tax incidence is:

$$
\frac{p_{b}-p^{*}}{p^{*}-p_{s}}=\frac{d t /(b+d)}{b t /(b+d)}=\frac{d}{b} .
$$

>.e. the part of tax paid by the buyer is higher, the larger the slope of the supply curve, $d$, and the smaller the slope of the demand curve, $b$.

## Tax Incidence and Own-Price Elasticities

By the definition of the (arc) own-price elasticity of demand:

$$
\begin{aligned}
\varepsilon_{D}=\frac{\frac{\Delta q}{q^{*}}}{\frac{\Delta p}{p^{*}}}=\frac{q^{t}-q^{*}}{q^{*}} & \frac{p^{*}}{p_{b}-p^{*}} \\
& \Rightarrow p_{b}-p^{*}=\frac{\left(q^{t}-q^{*}\right) \times p^{*}}{\varepsilon_{D} \times q^{*}} .
\end{aligned}
$$

## Tax Incidence and Own-Price Elasticities

By the definition of the (arc) own-price elasticity of supply:

$$
\begin{aligned}
\varepsilon_{S}= & \frac{\frac{\Delta q}{q^{\dot{*}}}}{\frac{\Delta p}{p^{*}}}=\frac{q^{t}-q^{\dot{*}}}{q^{\dot{*}}} \frac{p^{\dot{*}}}{p_{s}-p^{*}} \\
& \Rightarrow p_{s}-p^{\dot{*}}=\frac{\left(q^{t}-q^{*}\right) \times p^{\dot{*}}}{\varepsilon_{s} \times q^{*}} .
\end{aligned}
$$

# Tax Incidence and Own-Price Elasticities 

Tax incidence is $\frac{p_{b}-p^{*}}{p^{*}-p_{s}}=-\frac{\varepsilon_{s}}{\varepsilon_{D}}$.
The fraction of a $\$ t$ quantity tax paid by buyers (sellers) rises as supply becomes more (less) own-price elastic or as demand becomes less (more) ownprice elastic.

## Tax Incidence and

 Own-Price Elasticities

$$
q^{t} q^{*} \quad D(p), S(p)
$$

## Tax Incidence and

 Own-Price Elasticities

$$
q^{t}=q^{*} \quad D(p), S(p)
$$

# Deadweight Loss and Own-Price Elasticities 



## Deadweight Loss and Own-Price Elasticities


supply The tax reduces both CS and PS, transfers surplus to government, and lowers total surplus.
$D(p), S(p)$
Deadweight loss
(it is the inefficiency of the government intervension)

## Deadweight Loss and Own-Price Elasticities



## Deadweight Loss and Own-Price Elasticities



$$
q^{t} q^{*} \quad D(p), S(p)
$$

Deadweight loss give a good estimate of the efficiency cost of government policies

## Deadweight Loss and Own-Price Elasticities



## Deadweight Loss and Own-Price Elasticities

-Deadweight loss due to a quantity tax rises as either market demand or market supply becomes more ownprice elastic.

- If either $\varepsilon_{D}=0$ or $\varepsilon_{s}=0$ then the deadweight loss is zero.


## Long-Run Implications for Taxation

- In a short-run equilibrium, the burden of a sales or an excise tax is typically shared by both buyers and sellers, tax incidence of the tax depending upon the own-price elasticities of demand and supply.
- Q : Is this true in a long-run market equilibrium?


## Long-Run Implications for Taxation



## Long-Run Implications for Taxation



## The Effects of Subsidy

- A subsidy can be analyzed in much the same way as a tax
oPayment reducing the buyer's price below the seller's price
- It can be treated as a negative tax
-Quantity increases
- The benefit of the subsidy accrues mostly to buyers if $\mathrm{E}_{\mathrm{D}} / \mathrm{E}_{\mathrm{s}}$ is small


## Effects of a Subsidy



## Price Control and Surplus Changes



## Price Controls With Inelastic Demand

If demand is sufficiently


## Minimum Prices

- When price is set above the market clearing price:
-Quantity demanded falls
-Suppliers may, however, choose to increase quantity supplied in face of higher prices
- This causes additional producer losses equal to the total cost of production above quantity demanded

The deadweight loss given by triangles $\boldsymbol{B}$ and $\boldsymbol{C}$ results.

Increased price leading to decreased quantity by consumers equals area A

Consumers priced out of the market lose area B

PS increases from increased price for units sold equal to A

Losses for producers from drop in sales equal to C

Quantity

## Minimum Prices

## What if producers expand production to Q2

Price | from the increased price?


## Price Supports

- Much of agricultural policy is based on a system of price supports
-Prices set by government above free-market level and maintained by governmental purchases of excess supply
- Government can also increase prices through restricting production, directly or through incentives to producers


## Price Supports



Less costly is to simply give farmers the money

## Production Quotas

- The government can also cause the price of a good to rise by reducing supply
-Limitations of taxi license in a city
-Limitation of required liquor licenses for restaurants


## Supply Restrictions



## Supply Restrictions

Price
s' Government pays farmers not to produce more at the higher price
$S$
CS reduced by $\boldsymbol{A}+\boldsymbol{B}$

> | $\begin{array}{l}\text { Cost to } \\ \text { government }=\boldsymbol{B} \\ +C+D\end{array}$ |
| :--- |

Change in PS
D $=A-C+B+D+C$
Quantity

## Import Quotas and Tariffs

- Many countries use import quotas and tariffs to keep the domestic price of a product above world levels Olmport quotas: Limit on the quantity of a good that can be imported
- Tariff: Tax on an imported good
- This allows domestic producers to enjoy higher profits
-Cost to consumers is high


## Import Quotas and Tariffs

- With lower world price, domestic consumers have incentive to purchase from abroad
- Domestic price falls to world price and imports equal difference between quantity supplied and quantity demanded
- Domestic industry might convince government to protect industry by eliminating imports
-Quota of zero or high tariff


## Import Quotas to Eliminate Imports



