

Probability Calculus 2019/2020, Homework 7 (two problems)

Name and Surname ..... Student's number .....

*In the problems below, please use the following: as  $k$  – the sum of digits in your student's number; as  $m$  – the sum of the two largest digits in your student's number; and as  $n$  – the smallest digit in your student's number plus 1. For example, if an index number is 609999:  $k = 42$ ,  $m = 18$ ,  $n = 1$ .*

*Please write down the solutions (transformations, substitutions etc.), and additionally provide the final answer in the space specified (the answer should be a number in decimal notation, rounded to four digits).*

18. Monthly amounts of rainfall (measured in mm) in a sample of  $4m + 3$  regions were observed to be  $m, m + 1, \dots, 3m, 5k - 2m, 5k - 2m + 1, \dots, 5k$  and  $a$ , where  $a$  is a certain integer number. Knowing that the median of the sample amounts to  $3m + 1$ , find the value of the empirical CDF of the amount of rainfall at point  $5k - 3n + 1/2$ .

ANSWER:

Solution:

19. We have two boxes; there are  $m$  white balls and one black ball in the first box, and  $k$  white balls and one black ball in the second box. We randomly choose a box (each choice has the same probability) and then draw two balls simultaneously from the chosen box. Let  $X$  denote the number of black balls drawn, and  $Y$  denote the number of the box that was chosen. Find the correlation coefficient of variables  $X$  and  $Y$ .

ANSWER:

Solution: